UNIT



Just for Fun

Counting Rectangles

Challenge a classmate to see who can find the greatest number of rectangles in the room.

Set a time limit of 1 minute. Write down all the rectangles you can see.

At the end of 1 minute, exchange papers with your classmate.

Check each other's list.

Geometric Designer

Use only circles, triangles, rectangles, and parallelograms.

Draw any 3 of the following items:

- car, bus, truck, motorcycle
- person
- building
- animal
- landscape

Trade drawings with a classmate. Identify your classmate's drawings.

A Game for

Products and Factors

Work with a partner.

You will need two number cubes labelled 1 to 6 and 7 to 12, a pencil, and paper.



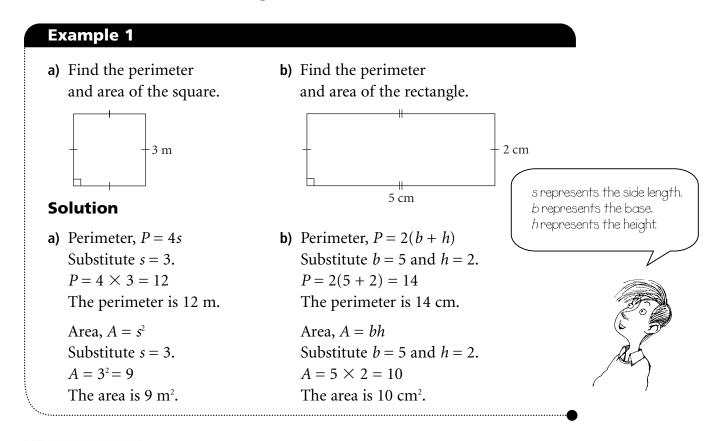


Take turns to roll the two cubes. Record the two numbers and find their product. In 10 seconds, write all the factors of that product that you can. Score 1 point for each factor you find. For which products did you score the fewest points? Why?

Activating Prior Knowledge

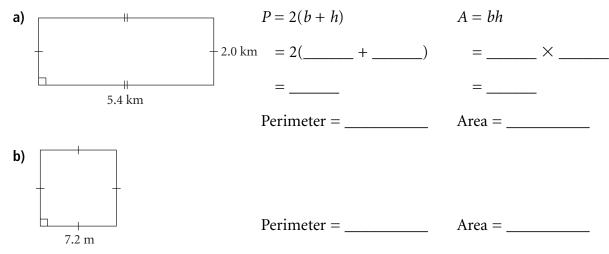
Perimeter and Area of a Rectangle

Perimeter is the distance around a shape. **Area** is the amount of surface a shape covers.



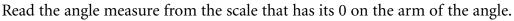


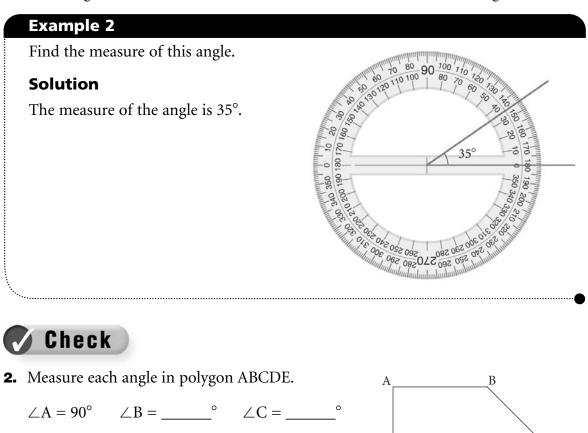
1. Find the perimeter and area of each shape.



Using a Protractor to Measure Angles

To measure an angle, place the base line of a protractor along one arm of the angle, with the centre of the protractor on the vertex of the angle.

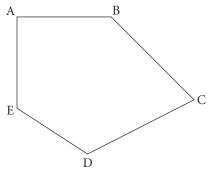




 $\angle D = \underline{\qquad}^{\circ} \quad \angle E = \underline{\qquad}^{\circ}$

Find the sum of the angles.

 $\angle A + \angle B + \angle C + \angle D + \angle E = ____°$



3. a) Use a ruler but not a protractor.Draw an angle that you think measures 75°.

b) Measure the angle with a protractor. How close was your angle to 75°?

Quick Review

4_1

► A circle is a closed curve. All points on the circle are the same distance from the centre of the circle. The distance between a point on a circle and the centre of the circle is a radius of the circle. The plural of radius is radii. The distance between two points on a circle through its centre is a **diameter** of the circle. ➤ The length of the diameter, *d*, of a circle is two times the length of the radius, r. That is, d = 2rAlso, the radius, r, of a circle is one-half the diameter, d. That is, $r = \frac{1}{2}d$, or $\frac{d}{2}$ You can find the radius of a circle, given the diameter.

For example, in a circle, *d* is 10 cm. Since $r = \frac{1}{2}d$, $r = \frac{1}{2} \times 10 = 5$ The radius is 5 cm.

You can find the diameter of a circle. given the radius.

radius

diameter

For example, in a circle, *r* is 4 cm. Since d = 2r, then $d = 2 \times 4 = 8$. The diameter is 8 cm.

•

Practice

- **1.** This circle has its centre at point O.
 - a) Draw a radius of the circle.

What is the length of the radius? _

b) Draw a diameter of the circle.

What is the length of the diameter?

2. From your results in question 1, write a relationship between the radius and the diameter of a circle.

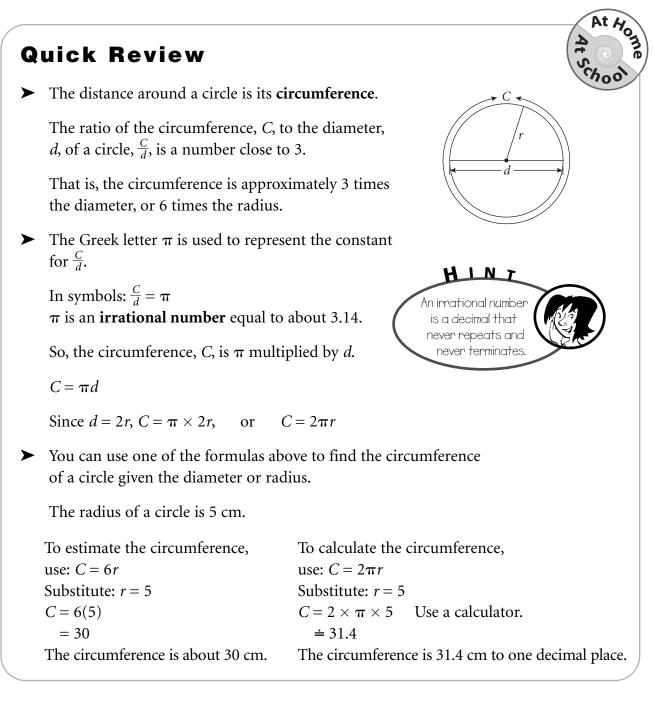
- **3.** Find the diameter of the circle with each radius.
 - a) 12 cm _____ b) 27 cm _____ c) 3.4 cm _____
- 4. Find the radius of the circle with each diameter.
 - a) 12 cm _____ b) 28 cm _____ c) 3.4 cm _____
- **5.** Write the steps you would take to draw a circle with radius 1 cm. Draw the circle.

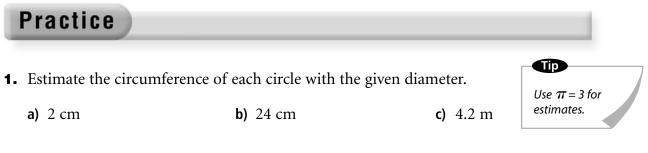
- **6.** Draw 4 radii in the circle you drew in question 5. What is the sum of the central angles of the circle? _____
- 7. Write the steps you would take to draw a circle with diameter 4 cm.

- **8.** Circular plates with diameter 20 cm are placed side by side on a table. The table measures 2.4 m by 1.2 m.
 - a) What is the length of the table in centimetres?
 - **b)** How many plates can fit side by side along the length of the table?
 - c) What is the width of the table in centimetres? _____
 - d) How many plates can fit side by side along the width of the table?
 - e) How many plates can fit on the table? _____
 - f) How many plates can fit around the perimeter of the table?

To convert metres to centimetres, multiply by 100.

4.2 Circumference of a Circle

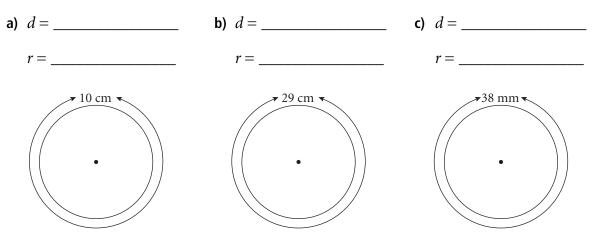




2. Estimate the circumference of each circle with the given radius.

	a) 2 cm	b) 24 cm	c) 4.2 m
3.	3. Calculate the circumference of each circle in question 2. Give the answers to one decimal place.		
a) $r = 2 \text{ cm}$ b) r		b) $r = 24$ cm	c) $r = 4.2 \text{ m}$

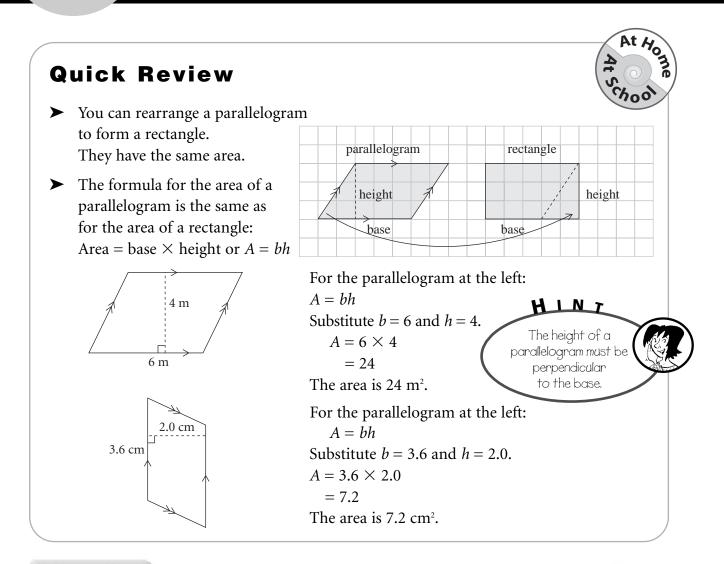
4. The circumference of each circle is given. Calculate the diameter and radius. Give the answers to one decimal place.



- **5.** A drinking glass has a circular base with a circumference of 21.4 cm.
 - a) Calculate the diameter of the circular base.
 - **b)** Circular coasters are made to extend beyond the edge of the glass base by 1 cm. What is the diameter of the coaster?
 - c) Calculate the circumference of the coaster.
- 6. A car tire has a radius of 36 cm. A stone gets stuck in the tire. How many times will the stone hit the ground when the car travels 1 km? Show your work.

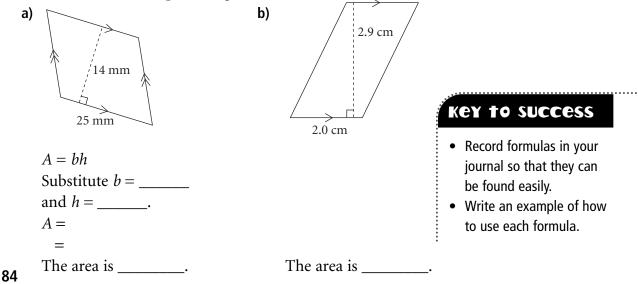


The stone will hit the ground ______ times.

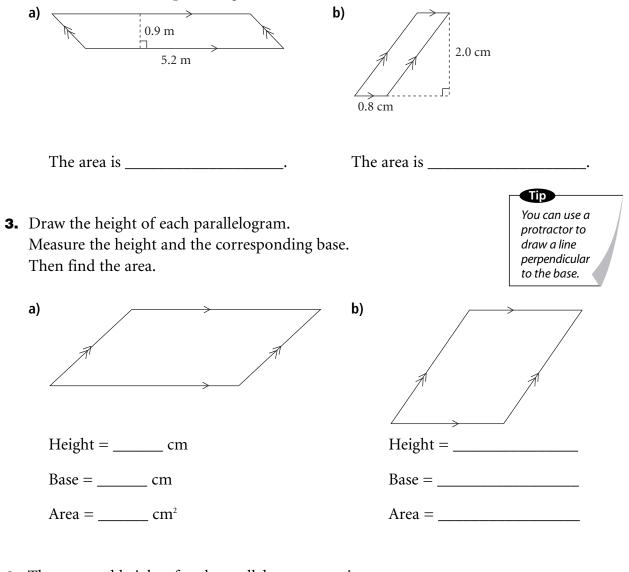


Practice

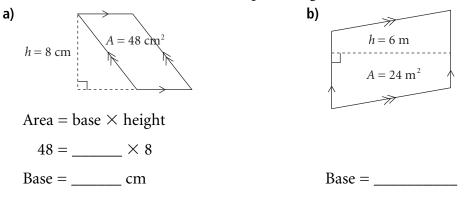
1. Find the area of each parallelogram.



2. Find the area of each parallelogram.



4. The area and height of each parallelogram are given. Find the measure of the base in each parallelogram.



5. a) On the grid below, draw 3 different parallelograms with base 6 units and height 2 units.



Find the area of each parallelogram.

b) On the grid above, draw a parallelogram with base 3 units and height 2 units.

Find its area.

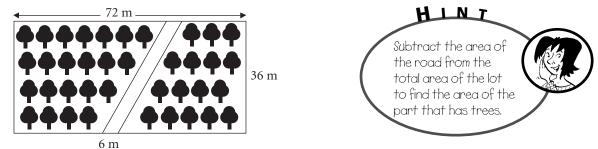
How does the area compare with the area of the parallelograms in part a?

c) On the grid above, draw a parallelogram with base 6 units and height 4 units.

Find its area.

How does the area compare with the area of the parallelograms in part a?

6. Jamie makes a road through his wooded lot. What is the area of the part of the lot that has trees? Show your work.

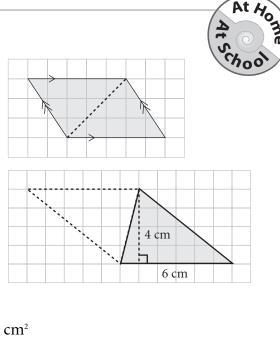


Quick Review

- This parallelogram has been divided into 2 congruent triangles. So, the area of one triangle is ¹/₂ the area of the parallelogram.
- To find the area of a triangle with base 6 cm and height 4 cm, complete a parallelogram on one side of the triangle.
- The area of the parallelogram is: $A = base \times height$ $A = 6 \times 4 = 24$

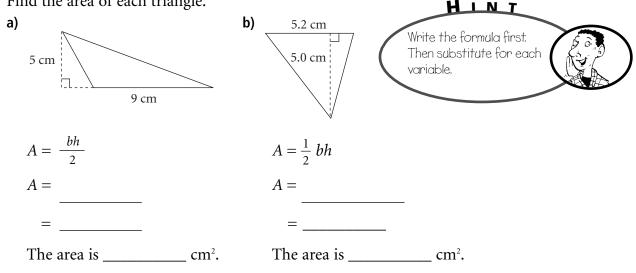
The area of the parallelogram is 24 cm². So, the area of the triangle is: $\frac{1}{2}$ of 24 cm² = 12 cm²

➤ You can use this formula for the area of a triangle. Area = $\frac{1}{2}$ base × height $A = \frac{1}{2} bh$ or $A = bh \div 2$ or $A = \frac{bh}{2}$



Practice

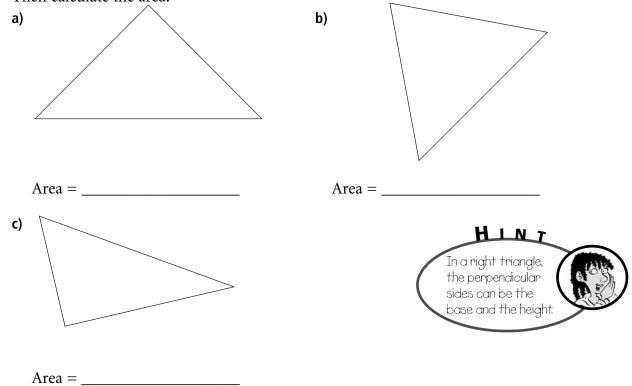
1. Find the area of each triangle.



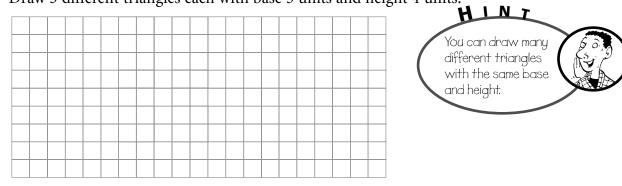
2. Find the area of each triangle.



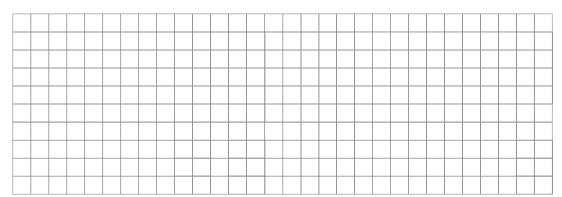
3. Measure and label the base and height of each triangle in centimetres. Then calculate the area.



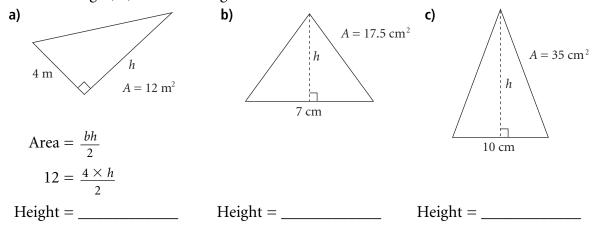
4. Draw 3 different triangles each with base 5 units and height 4 units.



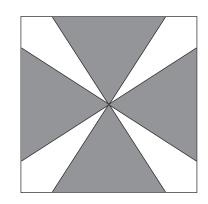
5. Draw 3 different triangles each with area 12 square units.



6. The area, *A*, of each triangle is given. Find the height, *h*, of each triangle.



7. Bernice makes this design on a square sheet of paper. The paper has a side length of 20 cm. Each triangle has a base of 12 cm and a height of 10 cm. Find the area of the white part of the design. Show your work.



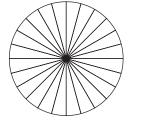


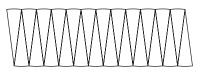
4.5 Area of a Circle

Quick Review



When a circle is divided into many congruent sectors, the sectors can be arranged to approximate a parallelogram.

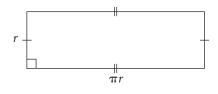


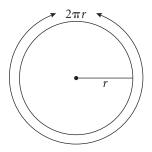


The more congruent sectors we use to divide the circle, the closer the area of the parallelogram is to the area of the circle.

For even greater numbers of sectors, the parallelogram approaches a rectangle. So, area of circle = area of rectangle

The sum of the 2 longer sides of the rectangle is equal to the circumference, *C*. Length of rectangle: $l = \frac{C}{2} = \frac{2\pi r}{2} = \pi r$ Each of the shorter sides is equal to the radius *r*. Width of rectangle: w = r





So, the area of a circle with radius *r* is: $A = l \times w$ $= \pi r \times r$

 \succ

 $=\pi r^2$

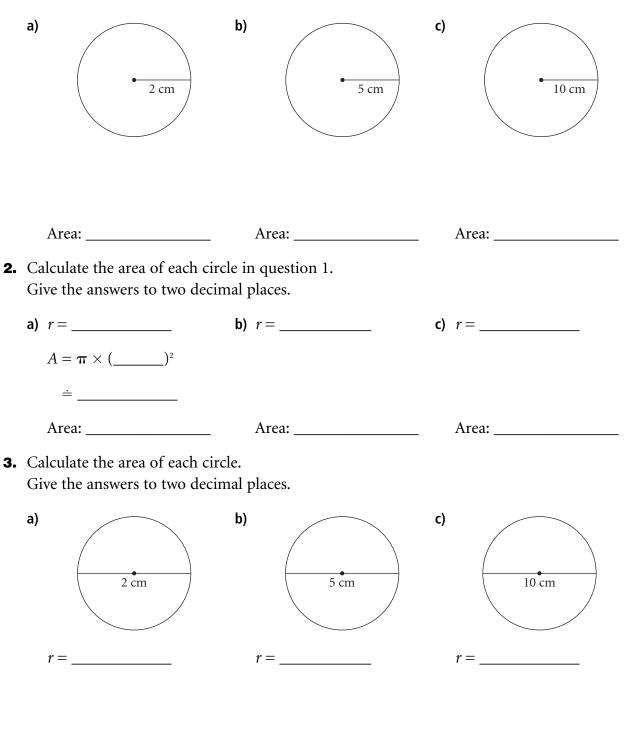
You can use the formula $A = \pi r^2$ to find the area of any circle given the radius *r*.

The	radius	of a	circle is	12 cm.	

To calculate the area, use: $A = \pi r^2$
Substitute: $r = 12$
$A = \pi \times 12^2$ Use a calculator.
≐ 452.389
The area is 452.39 cm ² to 2 decimal places.

Practice

1. Estimate the area of each circle.



4.	Use the results of questions 2 and 3.
	What happens to the area of a circle when
	its radius is doubled?



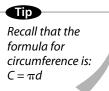
What happens to the area of a circle when its radius is halved?

- **5.** A machine is cutting circular coasters out of foam.
 - a) Each coaster has a diameter of 12 cm. What is its radius?
 - b) What is the area of each coaster?
 - c) Each piece of foam is a rectangle measuring 144 cm by 984 cm.

What is the area of the foam? _____

d) The coasters are cut with minimum waste.How many coasters can be cut from each piece of foam?

- e) What area of foam is wasted?
- **6.** The circumference of a circle is 92 cm. Calculate the area of the circle. Give the answer to one decimal place. Show your work.



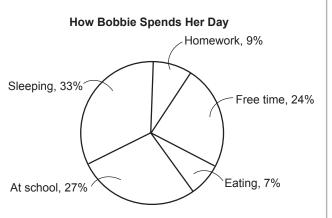
The area of the circle is ______.

Quick Review

4.6

A **circle graph** shows parts of one whole. This table and circle graph show how Bobbie spends a typical day.

Activity	Part of the day spent on each activity
Eating	7%
Free time	24%
Homework	9%
Sleeping	33%
At school	27%



The circle represents 100% of Bobbie's activities. The sum of the measures of the central angles is 360°.

Each sector of the circle represents a percent of the whole circle and a percent of Bobbie's day.

The circle graph has a title that describes what it represents.

When a computer is used to draw a circle graph, a legend shows what each sector represents.

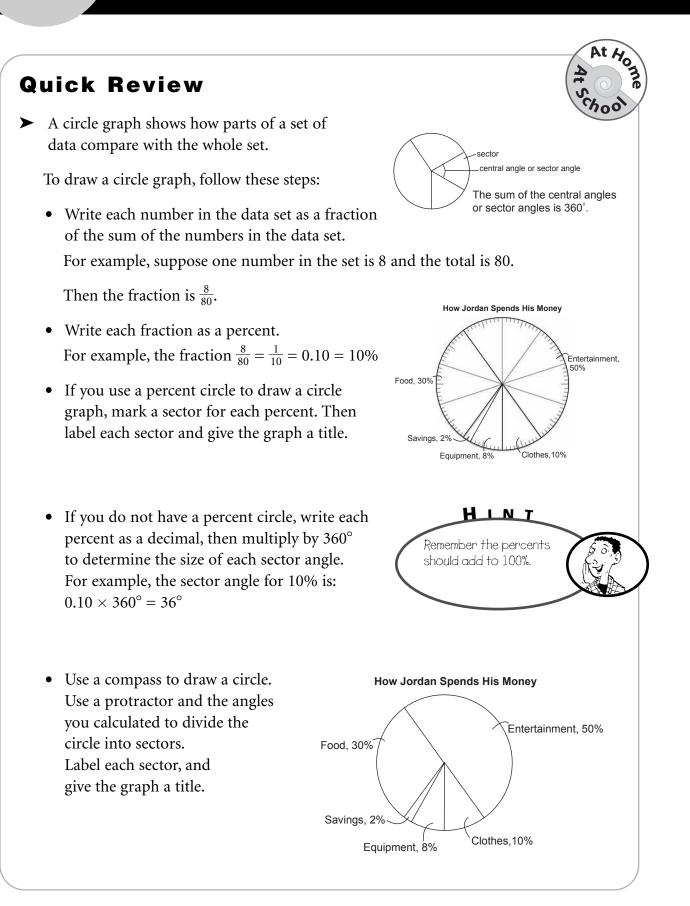
You can interpret the graph to find out about Bobbie's day:

- From the sizes of the sectors, you can see that Bobbie spent about 3 times as long at school as she did doing her homework.
- Also, the most time Bobbie spent doing any activity was sleeping. This was about one-third of the day.
- You can find how long Bobbie spent on any activity. There are 24 h in a day. Bobbie spent 9% of 24 h doing homework. This is: 0.09 × 24 h = 2.16 h So, Bobbie spent a little more than 2 h doing homework.

Practice

1.	On the 2006-07 Kootenay Junior Ice Hockey Team, there were 22 players. The circle graph shows where they came from.	Kootenay Ice Roster, 2006/2007
	 a) From which region do more players come than any other region? 	Alberta
	b) From which region do fewer players come than any other region?	
	c) From which two regions together do about one-half of the	British Columbia ne players come?
	d) Why is there a sector labelled "Other"?	
2.	Ms. Reid runs the local convenience store. She keeps track of the types of drinks she sells so she always The circle graph shows the drinks Ms. Reid sold in one week	
	a) Which drink was the most popular?	Drinks Sold in the Store / Juice, 15%
		Coffee, 35%
	b) Which drink was the least popular? E	inergy drinks, 10%
	c) Which two drinks together made up about one-half the sales?	Soft drinks, 20% Water, 20%
	d) Can you find out how much water Ms. Reid sold that wee	ek? Explain.
3.	This graph shows how the budget for the City of Winnipeg The budget for 2004 was \$692.9 million.	Was spent in 2004. City of Winnipeg 2004 Budget
	a) i) Which sector is the smallest?	
	ii) What does that tell you about how much money was spent for that sector?	Corporate offices, 14% Streets, waste management, 28%

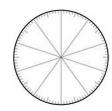
	b) H	low much money was spent on Police and fire services?
	c) i)	Which 3 sectors together are a little larger that the Police and fire services sector?
	ii	What does that tell you about how much money was spent on these 3 sectors?
	ii) How could you check your answer to part ii?
4.	He i	bel's father is preparing meals according to the guidelines of the Canada Food Guide. s planning a total of 25 servings per day, as shown in the graph. labelling is incomplete.
	a) V	That percent of the servings should be dairy products? Canada Food Guide
	H	low do you know? Meat/ alternatives, 12% Vegetables/ fruits, 32% Grains, 36%
	c) A	bout how many servings should be meat or meat alternatives?
	d) A	bout how many servings should be grains, or vegetables and fruits?
5.	telev	rvey was taken at school to determine the favourite genre of ision shows of the grade 7 students. One hundred twenty ents were surveyed. The results are shown in the graph.
	a) V	Thich genre had about one-third of the votes?
		Thich two genres together did one-quarter of the udents vote for? Reality/game, 25% Drama/soap, 20%
	c) V	Thich category received the fewest votes?
	V	/hy do you think that happened?
	d) H	low many students picked sports as their favourite?



Practice

1. Emily and Tasha checked the cars in the teachers' parking lot. The students grouped the cars according to where the headquarters of the manufacturer are located. Here are their data.

Origin of car	Number of cars
Asia (except Japan)	12
Europe	8
Japan	20
North America	10



- a) How many cars are in the lot? _____
- **b)** Write each type of car as a fraction of the total number of cars in the lot.
- c) Write each fraction in part b as a percent.
- d) Draw a circle graph in the percent circle.
- **2.** A group of grade 7 students was asked how many of Canada's other provinces and territories they have visited for at least one day. The data are shown below.

Number of provinces and territories visited	Number of students	Each number of students as a fraction of the total	Each fraction as a percent	Each percent as an angle
0	2			
1	4			
2 or 3	10			
4 to 6	5			
7 to 10	3			
11 or 12	1			

- a) Find the total number of students surveyed.
- **b)** Complete the table. For the last column, write each percent as a decimal, then multiply by 360°. Write each angle to the nearest degree where necessary.
- c) Draw and label a circle graph.

3. Here are data for the students who wrote Diploma Exams in Alberta, in 2004/2005:

Number of exams written	Percent of students	Each percent as an angle
0	18%	
1	4%	
2	13%	
3	12%	
4	19%	
5	21%	
6 or more	13%	

Alberta Diploma Exams Written, 2004/2005

- a) Draw and label a circle graph to display the data in the table.
- b) Approximately what fraction of the students wrote 4 or 5 exams? ______How do you know?
- **4.** The table below shows some First Nations' Treaties in Saskatchewan and the approximate percent of land area controlled within each treaty. The table is not complete.

Saskatchewan's First Nations' Land by Treaty

Treaty number	Land area as a percent	Sector angle in degrees
2	5%	
4		
5	3%	
6	25%	
8	14%	
10	32%	

- a) Find the percent of land controlled within treaty number 4. Complete the table.
- **b)** Display the data in a circle graph.
- c) Which treaty number controls one-quarter of the land?

How do you know? _____

d) Which treaty number controls about 4 times as much land as treaty number 2?

How do you know?



5. A group of adults was asked this question: "How do you regularly listen to music?" Here is what the adults said.

Category	Number of adults	Fraction of adults	Percent of adults	Each percent as an angle
CD	4			
MP3 player	12			
Radio	18			
Tape/walkman	4			
Vinyl	2			

Adults' Listening Preferences

- a) Complete the table.
- **b)** Draw a circle graph.
- c) Write, then answer a question about your graph.
- **6.** Matt loves to race his BMX bicycle.

Last summer, he attended a race in Kelowna, B.C. The registration in each class is given in the table below.

Class	Number of riders
20" elite women	19
20" elite men	65
20" elite junior women	31
20" elite junior men	96
Elite cruiser	29

- a) Display the data on a circle graph. Write the percents and angles to the nearest whole number where necessary.
- **b)** Colour the graph and include a legend.
- d) Write a question you could answer using your circle graph.

Answer your question.

In Your Words

Here are some of the important words of this unit.

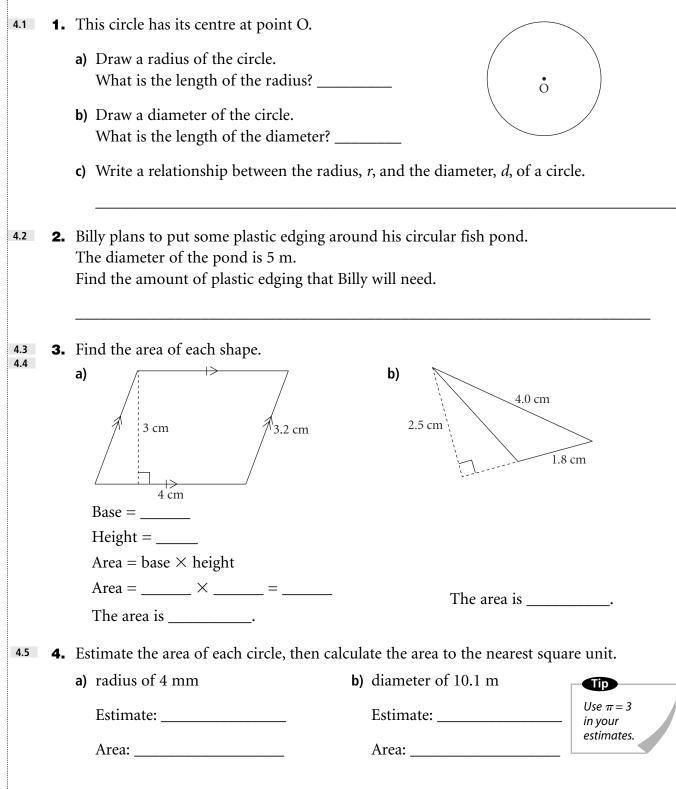
Build your own glossary by recording definitions and examples here. The first one is done for you.

radius_distance between	diameter	
a point on a circle and the centre of		
the circle		
For example,		
the radius of this 1 cm		
circle is 1 cm.		_
circumference	area of a circle	
		/
area of a triangle	circle graph	
		_

List other mathematical words you need to know.

Unit Review

LESSON



LESSON

- **5.** Kelly and her friends plan to start a rock band.
 - They will play in their town and in the surrounding area. The band has made this table to show its expenses as percents of what it will earn.

Type of Expense	Percent of budget	Each percent as an angle
Advertising	10%	
Clothes	20%	
Equipment	25%	
Food	15%	
Travel	30%	

Expenses of Kelly and the Rockers

- a) Complete the table.
- **b)** Draw and label a circle graph.
- c) The band estimates it will earn \$10 000 from its gigs. How much money will the band spend on food? _____
- d) Which type of expense is one-half the amount spent on clothes? ______ How can you tell this:

i) from the table?

ii) from the graph? _____

- e) The band wants to spend \$5000 on equipment upgrades.How much will the band have to earn to be able to do this? ______
- f) Write a question you can answer from the graph.
- g) Answer your question.