Fractions, Decimals, and Percents

Just for Fun

UNIT

3

Magic Square

In a Magic Square, the numbers in each row, column, and diagonal have the same sum, which is called the Magic Sum. Complete this Magic Square.

9.3	3.6	
	6.0	
		2.7

Magic Sum: _____

What Tree Is It?

What tree does a math teacher climb?

To solve the riddle:

- unscramble the letters in each row to form a math word
- for each word, circle the letter indicated in brackets

The circled letters will solve the riddle.

gaptinree		 	 	<u>C</u>		(last letter)
tvaeilnuqe	<u> </u>	 	 		-	(1st letter)
mnoocm	O	 				(2nd letter)
ledcima		 <u> </u>	 			(5th letter)
rotaremun		 	 			(4th letter)
ncafrtio		 <u> </u>	 			(5th letter)
dnmortaeino		 	 		<u> </u>	(last letter)
umltipyl		 	 			(last letter)

Activating Prior Knowledge

Mental Math

There are many ways to calculate mentally.

- Look for 10s, or the nearest 10.
- Add or subtract in a different order.
- Separate a number into smaller parts to obtain friendly numbers.

Example 1 Use mental math. a) 36 × 4 **b)** 403 + 55 - 4**c)** 305 + 498 I have a different approach Solution for part a. a) Separate 36 into 30 and 6: I know double 35 is 70, and double that is 140. Then I $30 \times 4 + 6 \times 4$ added 4 to get $36 \times 4 = 144$. = 120 + 24= 144**b)** Subtract first: **c)** 498 = 500 - 255 - 4 = 51Then: 305 + 500 - 2 = 803Then: 403 + 51 = 454🚺 Check **1.** Use mental math. a) $289 + 171 = 289 + ___ + 170$ **b)** 51 × 2 $50 \times 2 = _$ 1 × 2 = ____ = _____ + 170 =_____ **2.** Use mental math. Explain your strategy. **b)** 158 + 86 = _____ **c)** $34 \times 25 \times 4 =$ _____ a) $65 \times 3 =$ _____

Percent

Percent means "per hundred" or "out of 100." One whole, or 1, is 100%.

So: 25% is $\frac{25}{100}$ 4% is $\frac{4}{100}$ 100% is $\frac{100}{100}$ or 1

Example 2

This is a hundredths grid.

- a) What percent of the hundredths grid is shaded?
- **b)** What percent of the hundredths grid is not shaded?

Solution

a) 27 out of 100 squares are shaded.

$$\frac{27}{100} = 27\%$$

27% of the grid is shaded.

b) 73 out of 100 squares are not shaded.

 $\frac{73}{100} = 73\%$

73% of the grid is not shaded.



💋 Check

3. Write a fraction with denominator 100 for the shaded part of each hundredths grid. Then write each fraction as a percent.

a)



Quick Review

▶ $\frac{1}{4}$ is read as one-fourth, or one-quarter.

 $\frac{1}{4}$ means 1 divided by 4.

➤ To write a fraction as a decimal:

• Change the fraction to an equivalent fraction with a denominator of 10, 100, or 1000.

$$\frac{1}{4} = \frac{25}{100} = 0.25$$

• Or, divide the numerator by the denominator. 1 divided by 4

0.25 is a terminating decimal. It has a definite number of decimal places.

► Look at this fraction:

 $\frac{25}{99} = 0.252525 \ldots = 0.\overline{25}$

 $0.\overline{25}$ is a repeating decimal.

You draw a bar over the repeating digits.

► You can use patterns to change some decimals to fraction form.

Since
$$\frac{4}{9} = 0.\overline{4}$$
 $\frac{5}{9} = 0.\overline{5}$ $\frac{8}{9} = 0.\overline{8}$,

you can use the pattern to predict that the fraction for $0.\overline{2}$ is $\frac{2}{9}$.



Practice

1. Identify each decimal as terminating or repeating.



2. Match each fraction with its corresponding decimal.

$\frac{5}{9}$	0.16	Which fractions form terminating decimals?
$\frac{16}{99}$	0.5	
$\frac{1}{6}$	0.5	Which fractions form repeating decimals?
$\frac{5}{10}$	0.16	

3. Complete this table.

Fraction in simplest form				$\frac{12}{25}$		$\frac{9}{50}$
Fraction with denominator 10, 100, or 1000	$\frac{6}{10}$		$\frac{125}{1000}$			
Decimal		0.35			0.256	

- 4. Use a calculator to write each fraction as a decimal.
 - a) $\frac{2}{9}$ _____ b) $\frac{5}{8}$ _____ c) $\frac{5}{24}$ _____
- **5.** a) Express the fractions $\frac{8}{99}$, $\frac{9}{99}$, $\frac{10}{99}$, $\frac{11}{99}$, as decimals.



b) Describe the pattern in the decimals in part a.

c) Use the pattern to predict the decimal forms of $\frac{5}{99}$ and $\frac{21}{99}$.

Quick Review To order 3.25, $3\frac{1}{8}$, and $\frac{11}{3}$ from least to greatest: ► Use benchmarks on a number line. Compare the fraction parts of the numbers. 3.25 is halfway between 3 and 3.5. $3\frac{1}{8}$ is close to 3. $\frac{11}{3} = \frac{9}{3} + \frac{2}{3} = 3\frac{2}{3}$ $3\frac{2}{3}$ is greater than $3\frac{1}{2}$. $3 3^{1}_{8} 3.25 3^{1}_{2} = 3.5 1^{1}_{3}$ 4 So, from least to greatest: $3\frac{1}{8}$, 3.25, $\frac{11}{3}$ ► Use place value. Express each number as a decimal. Use a calculator. $3\frac{1}{8} = 3.125$ $\frac{11}{3} = 3.\overline{6}$ 3.25 Compare the digits, beginning with the greatest place value. In the ones place: 3.25, 3.125, and 3.6 have the same value, which is 3. In the tenths place: 1 tenth < 2 tenths < 6 tenths So, 3.125 < 3.25 < 3.6 So, from least to greatest: $3\frac{1}{8}$, 3.25, $\frac{11}{3}$ To write a fraction between $3\frac{1}{8}$ and $3\frac{1}{4}$: Since $3\frac{1}{4} = 3\frac{2}{8}$, find a fraction between $3\frac{1}{8}$ and $3\frac{2}{8}$. Write equivalent fractions with common denominator 16. $3\frac{1}{8} = 3\frac{2}{16} \qquad 3\frac{2}{8} = 3\frac{4}{16}$ Look at the numerators: 3 is between 2 and 4 So, $3\frac{3}{16}$ is between $3\frac{1}{8}$ and $3\frac{1}{4}$.

Practice

1. Use the number line to order each set of numbers from least to greatest.



 $\frac{7}{12}$, $\frac{5}{6}$, $\frac{3}{4}$, $\frac{2}{3}$



From greatest to least: _____

4. Use benchmarks and a number line to order each set of numbers from least to greatest.

a)
$$\frac{11}{12}$$
, $\frac{1}{3}$, $\frac{7}{6}$, $\frac{5}{4}$
 $\frac{1}{0}$, $\frac{1}{12}$, $\frac{1}{3}$, $\frac{7}{6}$, $\frac{5}{4}$

From least to greatest:



3.3

Quick Review ► Add: 5.763 + 3.94 **Step 1** Use front-end estimation to estimate the sum: 5 + 3 = 8Step 2 Add. Write each number with the same number of decimal places, using zeros as place holders. Record the numbers without the decimal points. 5763 +39409703 Since the estimate is 8, place the decimal point after the 9. The sum is 9.703. ► Subtract: 5.763 – 3.94 **Step 1** Use front-end estimation to estimate the difference: 5 - 3 = 2Step 2 Subtract. Write each number with the same number of decimal places, using zeros as place holders. Record the numbers without the decimal points. 5763 1823 Since the estimate is 2, place the decimal point after the 1. The difference is 1.823. Practice

1. Use front-end estimation to estimate each sum or difference.

a) 13.1 + 2.4 _____ b) 4.52 + 3.09 _____

c) 87.6 – 73.5 _____ d) 8.47 – 7.16 _____

2. Add. Use front-end estimation to place the decimal point.
a) 3.51 + 9.73
b) 2.168 + 0.948
c) 7.169 + 8.47
d) 6.7 + 0.491

Rewrite the question to make the calculation easier.

3. Subtract. Use front-end estimation to place the decimal point.

a) 9.73 - 0.41 b) 6.371 - 1.09 c) 4.152 - 4.097 d) 3.6 - 1.981

4.	The difference in the masses of 2 objects is 0.479 kg.
	a) What might the mass of each object be?
	b) What might the objects be?
5.	Salvatore ran 2.457 km on Saturday and 3.169 km on Sunday.
	a) Estimate to find out about how far he ran on both days.
	b) Calculate how far Salvatore ran on both days.
	c) Estimate how much farther he ran on Sunday than on Saturday.
	d) Calculate how much farther Salvatore ran on Sunday than on Saturday.
e	When the Andisons left on a trin the trin motor on their are showed (2590.2 km
0.	When they returned home, the trip meter showed 67178.4 km.
	a) Estimate to find the distance the Andisons drove on their trip.
	b) Calculate the distance the Andisons drove
7.	Silvia purchased these groceries: peanut butter for \$3.18, smoked turkey for \$5.43,
	bread for \$2.29, milk for \$1.89, and fish for \$6.79.
	a) Estimate to find the total cost of the groceries without tax.
	b) Calculate the total cost of Silvia's purchases.
	c) What is the difference in prices of the peanut butter and the fish?
	d) Silvia gave the clerk \$20.00. How much change should she receive?
8.	Paul packages boxes of apples for an orchard. In one hour, Paul lifted, weighed, and stored five boxes of apples with these masses: 9.71 kg, 9.39 kg, 8.97 kg, 8.72 kg, 8.98 kg
	a) Estimate to find the total mass.

b) Calculate the total mass.



Practice

1. Write a multiplication equation for each picture. Each small square represents 0.01.

a)



b)

- **2.** Use Base Ten Blocks to find each product. Record your work on the grid.
 - a) 2.6×1.3



b) 2.1×0.8



The product is _____.

c) 0.7×0.3

The product is _____.

- **3.** Multiply. Use front-end estimation to place the decimal point in the answer.
- a) 6.3×0.7 **b)** 1.8×1.4 Multiply: 63×7 Multiply: 18×14 63 \times 7 Estimate to place the decimal point. 6.3 × 0.7 = _____ $1.8 \times 1.4 =$ _____ **c)** 4.8×6 d) 3.4×2.1 **e)** 0.4×1.4 $4.8 \times 6 =$ ____ $3.4 \times 2.1 =$ ____ $0.4 \times 1.4 =$ ____ **4.** A rectangular room measures 2.3 m by 3.2 m. Find the area of the room. **5.** The product of 2 decimals is 0.24. Write 3 pairs of decimals that give this product.
- **6.** Chiang has a part-time job as a playground leader supervising children. Her hourly wage is \$9.25. She works 17.5 h per week.
 - a) Find Chiang's weekly wage.

Estimate: _____ Calculation: _____

b) How much money would Chiang earn in 5 weeks?_____

3.5



Practice

1. Write a division equation for this picture. Each small square represents 0.01.

- Use Base Ten Blocks to find each quotient. Record your work on the grid.
 - **a)** 0.8 ÷ 0.5

The quotient is:_____

b) 0.98 ÷ 0.7



The quotient is:_____

3. Divide.

a) 17.4 ÷ 2.4 b) 34.2 ÷ 3.6

 $17.4 \div 2.4$ is about

_____÷ _____= _____

So, 17.4 ÷ 2.4 = _____

So, 34.2 ÷ 3.6 = _____

c) 89.9 ÷ 3.1 = _____

d) 15.3 ÷ 6.8 = _____

4. Divide.

a) 452 ÷ 10 =	b) 89.12 ÷ 10 =
452 ÷ 100 =	89.12 ÷ 100 =
452 ÷ 1000 =	89.12 ÷ 1000 =
Describe any patterns you see.	
Divide.	
a) 452 ÷ 0.1 =	b) 89.12 ÷ 0.1 =
452 ÷ 0.01 =	89.12 ÷ 0.01 =
452 ÷ 0.001 =	89.12 ÷ 0.001 =
Describe any patterns you see.	
Divide. Estimate to place the decima	l point.
a) 3.9 ÷ 0.6	b) 6.2 ÷ 0.8
3.9 ÷ 0.6 is about:	6.2 ÷ 0.8 is about:
So, 3.9 ÷ 0.6 =	So, 6.2 ÷ 0.8 =
c) 8.51 ÷ 0.2	d) 6.7 ÷ 0.5
8.51 ÷ 0.2 is about:	6.7 ÷ 0.5 is about:
So, 8.51 ÷ 0.2 =	6.7 ÷ 0.5 =
A case of soup is on sale for \$18.63. There are 27 cans in a case.	
What is the cost of each can of soup	?

- **8.** Divide. Write each quotient to the nearest tenth if necessary.
 - a) $5.14 \div 1.07 =$ _____ b) $95 \div 5.4 =$ _____
 - c) $80.96 \div 41.8 =$ ____ d) $381.5 \div 2.4 =$ ____



9. Sheldon rode his bicycle 53.4 km in 3 days. He rode the same distance each day. How far did Sheldon ride in 1 day?

10. Nadine has a part-time job after school. She earns \$91.98 for working 12.6 h. How much does Nadine earn per hour? Use a calculator to find out.

11. The possible quotients for 72.09 ÷ 8.1 are: 0.89, 89, 890, and 8.9. Which number is correct? Explain how you know.

12. The area of a rectangular room is approximately 47.3 m². The width of the room is 5.4 m. Find the length of the room. Write your answer to the nearest tenth.

key to success

As you work through the Practice questions, ask:

- What have I learned?
- Do I understand?
- What am I not sure about?

At 4

Quick Review

You can use the same order of operations for decimals as you can for whole numbers.

Here is the order of operations.

- Do the operations in brackets first.
- Then divide and multiply, in order, from left to right.
- Then add and subtract, in order, from left to right.

Practice

1. Evaluate.

a) $1.2 + 3.1 \times 2 - (2.7 + 0.6) \div 3$	Calculate in brackets.
=	Multiply and divide from left to right.
=	Add and subtract from left to right.
=	
b) $9.9 + 5 \times 4.6$	c) $(6.2 - 2.6) \div 2 =$
=	
=	
Evaluate.	
a) $7 \times (6 + 7.1) =$	b) $16 - 9.6 \div 3.2 = _$
c) $5.8 + 12.3 \times 3 =$	d) 4.9 + 17.6 ÷ 8 =

2.

3. a) Evaluate each expression.

 $(5.3 + 7.5) \times (3 - 1) =$ _____ $5.3 + 7.5 \times 3 - 1 =$ _____

b) The numbers and operations are the same in the two expressions in part a. Explain why the results are different.

- **6.** A radio station contest used this skill-testing question: $4 + 6 \times 1.3 2.4 \div 2$ Grace said the answer was 10.6. Rob said the answer was 5.3. Who was correct? How do you know?



Practice

3.7

1. Use a fraction, decimal, and percent to describe the shaded part of each grid.

b)





2. Complete the chart.

Shape	Shaded region as a fraction	Shaded region as a decimal	Shaded region as a percent

3. Write each fraction as a decimal, and then as a percent. Use a calculator if necessary.



- **4.** Bennett had 19 out of 20 on a spelling test. Write Bennett's mark as a percent.
- **5.** In Ms. Khan's class, 22 out of 25 students hand in their projects on time. What percent of the students hand in their projects on time?
- **6.** Use 4 different colours to shade the squares on the hundredths grid below, as given in the table.

Describe each coloured part as a fraction, a decimal, and a percent.

Colour	Fraction	Decimal	Percent
Red	$\frac{6}{25}$		
Yellow			35%
Green		0.20	
Purple			18%
White			

7. Lucy and Victor are sharing pens.

Lucy has $\frac{1}{4}$ of the pens, and Victor has 20% of the pens. Who has more pens? Explain.

Since _____% > ____%, __

8. Raymond surveyed 10 classmates to find out which shoe, left or right, each person puts on first.

His results are shown in this table.

Left Shoe First	Right Shoe First
 	

a) What percent of the students surveyed put on their left shoe first?

- b) What percent of the students surveyed put on their right shoe first?
- 9. The Fashion Depot is having a big sale this week. Everything is $\frac{1}{5}$ off the regular price. What percent of the regular price do you pay? Explain. HINT The regular price is 100%. Write $\frac{1}{5}$ as a percent. Then, subtract from the regular price.

At A **Quick Review** HINT A scooter originally cost \$90.00. It is on sale at 40% off. To calculate a percent of a number, write the To find how much you save on the scooter, percent as a decimal. find 40% of \$90.00. $40\% = \frac{40}{100} = 0.40$ So, 40% of $90.00 = 0.4 \times 90$ To multiply $0.4 \times \$90$, multiply without the decimal point. 90 $\frac{\times 4}{360}$ Estimate to place the decimal point. \$90 is about \$100. 1% of \$100 is \$1. So, 40% of \$100 is \$40. Insert the decimal point between the 6 and the 0. So, 40% of \$90 is \$36.00. You save \$36 on the scooter. You can show this on a number line. \$<u>0</u> \$36 \$90 . 40%

Practice **1.** Find 10% of each number. **a)** 60 **b)** 85 $10\% \text{ of } 85 = \times =$ 10% of $60 = 0.1 \times 60 =$ **c)** 150 **d)** 55

100%

0%

2.	Find 30% of each number in quest	ion 1.	HINT
	a) 3 ×=	b) $3 \times ___=$	30% is 3x 10%
	30% of 60 =	30% of 85 =	
	c)	d)	
	30% of 150 =	30% of 55 =	
3.	Find each percent.		
	a) 7% of 80	b) 1% of 25.5	Tip The word "of" tells
	$7\% = \frac{7}{100} = $		you to multiply.
	× 80 =		
	c) 20% of 60.5	d) 37% of 182	

4. Asher's new backpack costs \$29.95, plus 14% sales tax.

a) How much sales tax does Asher pay? _____

b) How much does Asher pay in total for the backpack?

5. Here is a diagram of Sanjay's patio.What percent of the patio does the hot tub take up? Show your work.

	\backslash				

The hot tub takes up about _____ of Sanjay's patio.

6. Marco's dinner bill is \$14.80.

He leaves the server a 15% tip. How much does Marco pay for his dinner, including the tip? Show your work.

So, Marco paid _____ for his dinner.

- There are 620 students at Irena's school.
 Of these students, 45% have attended at least one other school.
 - a) How many students have attended more than 1 school?

So, ______ students have attended more than 1 school.

b) How many students have attended just 1 school?

So, ______ students have attended just 1 school.

8. Hraa has 120 baseball cards. She gives 25% of them away. How many cards does Hraa have left?

Hraa has _____ cards left.

9. Which would you rather have? Explain.90% of \$70 or 15% of \$500

In Your Words

Here are some of the important mathematical words of this unit.

Build your own glossary by recording definitions and examples here. The first one is done for you.

fraction	benchmark	
a way to show part of a whole; for		
example, $\frac{3}{4}$ shows 3 parts of a whole that		
has been divided into 4 equal parts		
A fraction also shows division: 3÷4	_	
equivalent fractions	repeating decimal	
	-	
	-	
	-	
	-	
terminating decimal	percent	
	-	
	-	

List other mathematical words you need to know.

Unit Review

LESSON



From least to greatest:

LESSO	N					
3.3	6.	Matthew bought a shirt for \$21.99, pants for \$36.78, and a belt for \$10.50.				
		What is the total amount for the purchases without sales tax?				
	7.	Kerry has grown 2.1 cm since last September. She is now 165 cm tall.				
		How tall was Kerry last September?				
3.4	8.	Multiply. Use front-end estimation to place the decimal point in the answer.				
		a) $0.5 \times 0.7 =$ b) $2.9 \times 0.8 =$				
		c) $3.5 \times 3.2 =$ d) $1.4 \times 2.9 =$				
	9.	Anne cycles 15.5 km each hour. She cycles for 3.25 h.				
		How far does Ann cycle?				
3.5	10.	Divide. Write each quotient to the nearest tenth where necessary.				
		a) $8.7 \div 0.6 = $ b) $5.7 \div 1.5 = $				
		c) $43.1 \div 2.1 = ___$ d) $23.5 \div 4.8 = ___$				
	11.	Amal bought 3.5 kg of bananas for \$2.42.				
		What was the cost of 1 kg of bananas?				
1						

LESSON

3.6	12.	Evaluate.		Tip
		a) 5.3 − 2.3 × 2 =	b) (67.2 + 12) ÷ 2.4 – 1.2 =	The order of operations with decimals is the same as with whole numbers.
3.7	13.	Write each fraction as a	decimal and a percent.	
		a) $\frac{1}{2} = __=$	b) $\frac{17}{25} = \underline{\qquad} = \underline{\qquad}$	
		c) $\frac{19}{20} = ___=$	d) $\frac{3}{5} = ___=$	
3.8	14.	Ivana got $\frac{21}{25}$ on her scie	ence test.	
		She got 86% on her mat	h test.	
		Which of her test marks	is greater? Explain.	
		Ivana's	_ test mark is greater.	
	15.	Find each percent.		
		a) 3% of 25	b) 24% of \$9.00	c) 40% of 95
		$3\% = \frac{3}{100} = 0.03$	24% =	
		0.03 × 25 =		
	16.	Sylvia is going to buy a 1 The regular price is \$68. The jacket is on sale for There is 14% sales tax of How much will Sylvia pa	new jacket. 00. 25% off. n the jacket. ay for the jacket?	

Sylvia will pay _____ for the jacket.